

A VERY EASY AND  
SHORT METHOD

OF FINDING THE

TRUE DISTANCE

BETWEEN THE

MOON and the SUN, or a fixed STAR,

FOR THE PURPOSE OF DETERMINING THE

LONGITUDE.

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# P R E C E P T.

WITH the moon's apparent altitude and horizontal parallax, to be found in the Nautical Almanack, page 7, take the logarithm out of Table 9, Requisite Tables, which reserve, and also the correction of her altitude from Table 8, Requisite Tables; to this add the refraction of the star from Table 1, Requisite Tables, or, if the observation be taken from the sun, the difference between the sun's parallax \* and refraction; which, if the altitude of the sun or star be greater than that of the moon, take from the difference of the apparent altitudes; but add them together, if the altitude of the moon be the greater, and you will have the difference of the true altitudes, of which take half. Then to the logarithm from Table 9, Requisite Tables, add the logarithmic sine of the half sum of the difference or the apparent altitudes and apparent distance, the logarithmic sine of half their difference, and reject radius; double the logarithmic sine of the half difference of the true altitudes, and, if this double logarithmic sine be less than the logarithmic sum radius rejected (above-mentioned) take it from that; but, if greater, take the logarithmic sum radius rejected from it; then find the nearest logarithm to this logarithmic remainder, but under, from a table of common logarithms, and note the correspondent number to four places; take that logarithm from this, and reserve the remainder, to the noted correspondent number add 1, then seek the logarithm answering to this sum, and to this logarithm add a difference to be taken out of the Table of Multipliers, pages 4 and 5, (as directed in page 3,) and halve the same. And if double the logarithmic sine of the half difference of the true altitudes be less than the logarithmic sum radius rejected (above-mentioned) add the logarithmic sine of the half difference of the true altitudes to this half, and this last logarithmic sum will be <sup>the</sup> logarithmic sine of half of the true distance.

But, if the logarithmic sum radius rejected (before-mentioned) be less than double the logarithmic sine of the half difference of the true altitudes, (+ See Example 9,) to the above-mentioned half logarithm, add half the logarithmic sum radius rejected (above-mentioned) and this last logarithmic sum will be the logarithmic sine of half of the true distance.

\* The sun's parallax in altitude is in Table 3, Requisite Tables.

N.B. — How the longitude may be determined by the help of the true distance between the moon and the sun, or a fixed star, it shewn in every modern Epitome of Navigation.



## The Explanation of the Table of Multipliers.

**T**HE columns marked at the top Num. contain numbers beginning at 1,000 and ending at 8,999: Those marked Mult. contain the multiplier correspondent to each number opposite, and to the intermediate numbers. The column marked Diff. following, contains the differences to logarithms of seven places besides the index, correspondent to each number opposite, and to the intermediate numbers, from 9,000 to 9,999, and the column next to it contains also the multiplier correspondent to each number opposite, and to the intermediate numbers.

What has been said here sufficiently explains the rest of the Table.

*Method of finding the Difference from this Table, which is to be added to the Logarithm answering to the noted correspondent Number increased by 1, mentioned in the Precept preceding.*

**DIRECTION I.** From 1,000 to 8,999, (inclusive) also from 10,00 to 68,49, (inclusive) and from 100,0 to 201,9, (inclusive) the product of the reserved remainder by the multiplier correspondent to the number answering to the logarithmic remainder, (mentioned in the precept) cutting off two figures to your right hand, is the difference.

**DIRECTION II.** From 9,000 to 9,999, (inclusive) also from 99,00 to 99,99, (inclusive) and from 999,0 to 999,9, (inclusive) multiply the difference in this table, answering to the number correspondent to the logarithmic remainder, (mentioned in the precept) by the fourth figure of that number; to this add the reserved remainder; the product of this sum by the multiplier, correspondent to the number answering to the logarithmic remainder, (mentioned in the precept) cutting off two figures to your right hand, is the difference.

**DIRECTION III.** From 63,50 to 98,99, (inclusive) and from 203,0 to 998,9, (inclusive) add the reserved remainder to the logarithm correspondent to the number answering to the logarithmic remainder, (mentioned in the precept) increased by 1.

**DIRECTION IV.** When the index of the logarithmic remainder (mentioned in the precept) is 3, to the logarithmic remainder add the difference between the next logarithm under the logarithmic remainder in a table of common logarithms, and the next greater; then, the half of this last logarithm is to be added either to the logarithmic sine of the half difference of the true altitudes, or to half of the logarithmic sum radius rejected (mentioned in the precept) as there directed.

**DIRECTION V.** When the index of the logarithmic remainder (mentioned in the precept) is 4, to the logarithmic remainder add one-tenth of the difference between the next logarithm under the logarithmic remainder, in a table of common logarithms, and the next greater; then the half of this last logarithm is to be added either to the logarithmic sine of the half difference of the true altitudes, or to half of the logarithmic sum radius rejected (mentioned in the precept) as there directed.

**DIRECTION VI.** When the index of the logarithmic remainder (mentioned in the precept) is 5, to the logarithmic remainder add one hundredth of the difference between the next logarithm under the logarithmic remainder, in a table of common logarithms, and the next greater; then the half of this last logarithm is to be added either to the logarithmic sine of the half difference of the true altitudes, or to half of the logarithmic sum radius rejected (mentioned in the precept) as there directed.

**DIRECTION VII.** When the index of the logarithmic remainder (mentioned in the precept) is 6, or upwards, add the half of the logarithmic remainder either to the logarithmic sine of the half difference of the true altitudes, or to half of the logarithmic sum radius rejected (mentioned in the precept) as there directed.



Num.	Mult.	Num.	Mult.	Num.	Mult.	Num.	Mult.	Num.	Mult.	Num.	Mult.	Num.	Mult.	Num.	Mult.	Num.	Diff.*	Mult.	Num.	Mult.
1,000	,50	2,189	,68	3,089	,75	3,869	,79	4,809	,83	5,919	,86	7,279	,87	9,000	48,3	,90	10,00			
1,029	,51	2,199	,69	3,099	,76	3,909	,80	4,839	,82	5,959	,85	7,309	,88	9,119	47,6	,89	10,89			
1,079	,52	2,279	,70	3,239	,77	3,919	,79	4,859	,83	5,999	,86	7,429	,90	9,149	47,4	,91	12,09			
1,119	,53	2,289	,69	3,249	,76	3,939	,80	4,969	,84	6,069	,85	7,449	,88	9,219	47,1	,90	12,49			
1,159	,54	2,299	,70	3,259	,77	3,969	,79	4,999	,83	6,079	,86	7,559	,89	9,329	46,6	,89	13,69			
1,199	,55	2,399	,71	3,309	,76	3,979	,80	5,029	,84	6,169	,87	7,609	,88	9,359	46,4	,91	13,29			
1,259	,56	2,489	,72	3,339	,77	4,009	,81	5,079	,83	6,179	,86	7,699	,89	9,429	46,1	,90	13,39			
1,319	,57	2,499	,71	3,349	,76	4,029	,80	5,089	,84	6,249	,87	7,749	,88	9,549	45,5	,89	13,79			
1,359	,58	2,509	,72	3,359	,77	4,129	,81	5,149	,85	6,309	,86	7,839	,89	9,559	45,4	,92	13,89			
1,409	,59	2,629	,73	3,439	,78	4,149	,80	5,169	,83	6,349	,87	7,959	,87	9,569	45,4	,91	13,99			
1,479	,60	2,639	,72	3,459	,77	4,169	,81	5,209	,84	6,429	,85	7,979	,89	9,599	45,0	,90	14,49			
1,549	,61	2,649	,73	3,469	,78	4,269	,80	5,249	,83	6,489	,87	8,129	,91	9,769	44,4	,92	14,69			
1,609	,62	2,729	,74	3,509	,77	4,289	,81	5,269	,84	6,539	,88	8,149	,89	9,789	44,4	,91	14,90			
1,679	,63	2,739	,73	3,529	,78	4,309	,82	5,339	,85	6,559	,86	8,279	,90	9,799	44,3	,92	15,09			
1,739	,64	2,789	,74	3,579	,79	4,339	,81	5,349	,84	6,639	,88	8,359	,88	9,809	44,3	,91	15,59			
1,749	,63	2,899	,75	3,609	,78	4,349	,82	5,409	,85	6,699	,86	8,449	,90	9,899	43,9	,90	16,69			
1,759	,64	2,909	,74	3,639	,79	4,469	,81	5,439	,84	6,739	,88	8,559	,88	9,909	43,8	,91	16,79			
1,829	,65	2,949	,75	3,659	,78	4,509	,82	5,469	,85	6,839	,86	8,609	,90	9,919	43,8	,90	16,89			
1,889	,66	3,009	,74	3,679	,79	4,539	,81	5,639	,84	6,849	,87	8,749	,92	9,999	43,4	,92	16,99			
1,989	,67	3,019	,75	3,759	,78	4,559	,82	5,699	,86	6,959	,89	8,769	,90				17,10			
2,069	,68	3,029	,75	3,769	,79	4,659	,83	5,739	,84	6,979	,87	8,959	,92	99,00	43,8	,99	17,20			
2,079	,67	3,039	,76	3,799	,80	4,699	,82	5,759	,85	7,069	,89	8,999	,90	99,29	43,7	,98	17,40			
2,089	,68	3,049	,75	3,809	,79	4,709	,83	5,839	,86	7,129	,87			99,99	43,4	1,00	17,60			
2,179	,69	3,079	,76	3,839	,80	4,759	,82	5,849	,85	7,179	,88</									

DIRECTION VII. When the index of the logarithmic remainder (mentioned in the process) is 6 or upwards, add the half of the logarithmic remainder either to the logarithmic part of the true remainder, or to the difference of the true remainder and the logarithmic remainder (mentioned in the process) as there directed.

DIRECTION VIII. When the index of the logarithmic remainder (mentioned in the process) is 6 or upwards, add the half of the logarithmic remainder either to the logarithmic part of the true remainder, or to the difference of the true remainder and the logarithmic remainder (mentioned in the process) as there directed.

DIRECTION VI. When the index of the logarithmic remainder is 5, add the logarithmic remainder to the logarithmic remainder, and the next greater, then the half of the logarithmic remainder is to be added either to the logarithmic part of the true remainder, or to half of the logarithmic remainder (mentioned in the process) as there directed.

DIRECTION V. When the index of the logarithmic remainder (mentioned in the process) is 4, to the logarithmic remainder add one-fourth of the difference between the next logarithmic remainder, to a table of common logarithms, and the next greater, then the half of the logarithmic remainder is to be added either to the logarithmic part of the true remainder, or to half of the logarithmic remainder (mentioned in the process) as there directed.



# M U L T I P L I E R S.

Mult.	Nam.	Mult.	Nam.	Mult.	Nam.	Mult.	Nam.	Mult.	Nam.	Mult.	Nam.	Mult.	Nam.	Mult.	Nam.
.90	10.00	.91	21.89	.95	30.79	.97	36.39	.97	48.59	.99	56.99	.99	60.9	.99	60.9
.89	10.89	.92	22.19	.96	30.89	.96	37.99	.98	48.69	.98	57.39	.97	62.9	1.00	1.00
.91	11.09	.93	22.59	.95	30.99	.97	38.09	.97	49.19	.99	57.59	.99	63.9	.99	63.9
.90	11.49	.92	22.69	.96	31.39	.96	38.69	.98	49.29	.98	58.19	.97	65.9	1.00	1.00
.89	11.69	.93	25.09	.97	31.49	.97	38.79	.97	49.69	.99	58.39	.99	66.9	.99	66.9
.91	11.29	.92	25.19	.96	31.59	.96	39.39	.98	49.89	.98	58.99	.97	67.9	1.00	1.00
.90	11.39	.93	26.59	.97	31.69	.97	39.49	.97	50.29	.99	59.19	.99	68.9	.99	68.9
.89	11.79	.94	26.69	.96	33.59	.98	39.79	.98	50.49	.98	59.79	.97	70.9	1.00	1.00
.92	11.89	.93	26.79	.97	33.69	.97	39.89	.97	50.89	.99	59.99	.99	71.9	.99	71.9
.91	11.99	.94	26.89	.96	33.89	.98	40.09	.98	51.09	.98	60.69	.97	72.9	1.00	1.00
.90	12.49	.93	27.09	.97	33.99	.97	40.29	.97	51.49	.99	60.79	.99	75.9	.99	75.9
.92	12.69	.94	27.19	.96	34.19	.98	40.49	.98	52.39	.98	61.49	.97	76.9	1.00	1.00
.91	12.99	.93	27.29	.97	34.29	.97	40.69	.97	52.69	.99	61.69	.99	77.9	.99	77.9
.92	13.09	.94	27.39	.96	34.39	.98	40.89	.98	53.09	.98	63.39	.97	78.9	1.00	1.00
.91	13.59	.95	27.49	.97	34.59	.97	41.09	.97	53.39	.99	63.49	.99	80.9	.99	80.9
.90	13.69	.94	27.59	.96	34.69	.98	41.29	.98	53.69	.98	100.0	.99	81.9	1.00	1.00
.91	13.79	.95	27.69	.97	34.79	.97	41.49	.97	54.09	.99	100.0	.99	83.9	.99	83.9
.90	13.89	.94	27.79	.96	34.99	.98	41.69	.98	54.39	.99	142.9	.99	84.9	1.00	1.00
.92	13.99	.95	27.89	.97	35.19	.97	41.89	.97	54.69	.99	144.9	.99	87.9	.99	87.9
.91	14.19	.94	28.49	.96	35.29	.98	42.89	.98	55.09	.98	148.9	.99	88.9	1.00	1.00
.90	14.29	.95	28.59	.97	35.39	.97	43.49	.99	55.39	.99	149.9	.99	90.9	.99	90.9
.92	14.49	.94	28.69	.96	35.59	.98	43.59	.98	55.69	.99	155.9	.99	91.9	1.00	1.00
1.00	14.69	.95	28.79	.97	36.09	.97	44.89	.99	56.09	.99	156.9	.99	92.9	.99	92.9
1.00	14.99	.96	30.69	.96	36.19	.98	44.89	.98	56.59	.99	159.9	.99	93.9	1.00	1.00



( 6 )

## EXAMPLE I.

Let the apparent distance of the moon's center from a star be  $51^{\circ} 28' 35''$  when the star's apparent altitude was  $24^{\circ} 48'$  the moon's apparent altitude  $12^{\circ} 30'$  and her horizontal parallax  $56' 15''$ . Required Their true Distance.

Star's apparent altitude,	$24^{\circ} 48'$	Apparent distance,	$51^{\circ} 28' 35''$	Logarithm from Tab. 9, } Req. Tab.	9,99865
Moon's - - - - -	$12^{\circ} 30'$	Diff. of apparent altitudes	$12^{\circ} 18' 0''$		
Difference of apparent altitudes,	$12^{\circ} 18'$	Sum	$63^{\circ} 46' 35''$	Half is $31^{\circ} 53' 18''$ log. fine	9,72285
Correction from tab. 8, Req. Tab.	$50' 42''$	Difference	$39^{\circ} 10' 35''$	Half is $19^{\circ} 35' 18''$ log. fine	9,52538
Star's refraction tab. 1, Req. Tab.	$2' 3''$	Logarithmic sum radius rejected	- - - - -	- - - - -	19,24688
Difference of true altitudes,	$11^{\circ} 25' 15''$	$5^{\circ} 42' 37\frac{1}{2}'' =$ log. fine	8,99783, which multiplied by 2 is		17,99566
Half difference is - - -	$5^{\circ} 42' 37\frac{1}{2}''$			* 17,83 = 1,25122 18,83 = 1,27492	
* This falls in with direction 1st of the Table of Multipliers. }		Half the above logarithm is		0,63746	
		Half difference of true altitudes, log. fine		8,99783	
	$25^{\circ} 34' 56''$ $\frac{2}{2}$			log. fine	9,63529
	$51^{\circ} 9' 52''$	True Distance.			

## EXAMPLE II.

Let the apparent distance of the moon's center from the sun's be  $59^{\circ} 25' 34''$  when the sun's apparent altitude was  $59^{\circ} 12'$ , the moon's apparent altitude  $27^{\circ} 2'$  and her horizontal parallax  $59' 58''$ . Required their True Distance.

Sun's apparent altitude,	$59^{\circ} 12'$	Apparent distance,	$59^{\circ} 25' 34''$	Logarithm from tab. 9, } Req. Tab.	9,996719
Moon's - - - - -	$27^{\circ} 2'$	Diff. of apparent altitudes,	$32^{\circ} 10' 0''$		
Difference of apparent altitudes,	$32^{\circ} 10'$	Sum	$91^{\circ} 35' 34''$	Half is $45^{\circ} 47' 47''$ log. fine	9,855438
Correction from tab. 8, Req. Tab.	$51' 33''$	Difference	$27^{\circ} 15' 34''$	Half is $13^{\circ} 37' 47''$ log. fine	9,372260
Sun's refraction tab. 1, Req. Tab. $34''$ }		Logarithmic sum radius rejected	- - - - -	- - - - -	19,224417
Sun's paral. in alt. tab 3, Req. Tab. 4 }	$30''$	$15^{\circ} 38' 59'' =$ log. fine	9,430970, which multiplied by 2 is		18,861940
Difference of true altitudes,	$31^{\circ} 17' 57''$			* 2,303 = 0,362477 3,303 = 0,519037	
Half difference is - - -	$15^{\circ} 38' 59''$			Half the above logarithm is	0,259519
* This falls in with direction 1st of the Table of Multipliers. }		Half difference of true altitudes, log. fine		9,430970	
	$29^{\circ} 21' 44''$ $\frac{2}{2}$			log. fine	9,690489
	$58^{\circ} 43' 28''$	True Distance.			

## EXAMPLE III.

Let the apparent distance of the moon's center from a star be  $46^{\circ} 20'$  when the star's apparent altitude was  $19^{\circ} 12'$ , the moon's apparent altitude  $32^{\circ} 14'$  and her horizontal parallax  $55^{\circ} 12'$ . Required their True Distance.

Moon's apparent altitude,	$32^{\circ} 14'$	Apparent distance,	$46^{\circ} 20'$	Logarithm from tab. 9, } Req. Tab.	9,996468
Star's - - - - -	$19^{\circ} 12'$	Diff. of apparent altitudes,	$13^{\circ} 2'$		
Difference of apparent altitudes,	$13^{\circ} 2'$	Sum	$59^{\circ} 22'$	Half is $29^{\circ} 41'$ log. fine	9,694786
Correction from tab. 8, Req. Tab.	$45' 11''$	Difference	$33^{\circ} 18'$	Half is $16^{\circ} 39'$ log. fine	9,457162
Star's refraction tab. 1, Req. Tab.	$2' 42''$	Logarithmic sum radius rejected	- - - - -	- - - - -	19,148416
Difference of true altitudes,	$13^{\circ} 49' 58''$	$6^{\circ} 54' 57'' =$ log. fine	9,080667, which multiplied by 2 is		18,161334
Half difference is - - -	$6^{\circ} 54' 57''$			* 9,706 = 0,987082 10,70 = 1,029664	
* This falls in with direction 2d of the Table of Multipliers. }		Half the above logarithm is		0,514832	
		Half difference of true altitudes, log. fine		9,080667	
	$23^{\circ} 12' 14''$ $\frac{2}{2}$			log. fine	9,595499
	$46^{\circ} 21' 28''$	True Distance.			



# EXAMPLE IV.

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Let the apparent distance of the moon's center from a star be  $120^{\circ} 0'$  when the star's apparent altitude was  $14^{\circ} 30'$ , the moon's apparent altitude  $20^{\circ} 26'$ , and her horizontal parallax  $54' 16''$ . Required their True Distance.

Star's apparent altitude,	$24^{\circ} 30'$	Apparent distance,	$120^{\circ} 0'$	Logarithm from Tab. 9,	
Moon's	$20^{\circ} 26'$	Diff. of apparent altitudes,	$4^{\circ} 4'$	Req. Tab.	9.997795
Difference of apparent altitudes,	$4^{\circ} 4'$	Sum	$124^{\circ} 4'$	Half is $62^{\circ} 2'$ log. fine	9.946069
Correction from tab. 8, Req. Tab.	$48' 19''$	Difference	$115^{\circ} 56'$	Half is $57^{\circ} 58'$ log. fine	9.931823
Star's refraction tab. 1, Req. Tab.	$2^{\circ} 4'$	Logarithmic sum radius rejected			19.872125
Difference of true altitudes,	$3^{\circ} 13' 37''$	$1^{\circ} 36' 49'' = \log. \text{ fine } 8.449615$ , which multiplied by 2 is			16.899230
Half difference is	$1^{\circ} 36' 49''$				
* This falls in with direction 3d of the Table of Multipliers.	$59^{\circ} 43' 8''$			Half the above logarithm is	1.486679
	$2$			Half difference of true altitudes, log. fine	8.449615
	$119^{\circ} 26' 16''$	True Distance,		log. fine	9.935294

# EXAMPLE V.

Let the apparent distance of the moon's center from a star be  $96^{\circ} 4'$  when the star's apparent altitude was  $13^{\circ} 32'$ , the moon's apparent altitude  $40^{\circ} 24'$  and her horizontal parallax  $54' 22''$ . Required their True Distance.

Star's apparent altitude,	$43^{\circ} 32'$	Apparent distance,	$96^{\circ} 4'$	Logarithm from Tab. 9,	
Moon's	$40^{\circ} 24'$	Diff. of apparent altitudes,	$3^{\circ} 8'$	Req. Tab.	9.995737
Difference of apparent altitudes,	$3^{\circ} 8'$	Sum	$99^{\circ} 12'$	Half is $49^{\circ} 36'$ log. fine	9.881692
Correction from tab. 8, Req. Tab.	$40' 16''$	Difference	$92^{\circ} 56'$	Half is $46^{\circ} 28'$ log. fine	9.860322
Star's refraction, tab. 1, Req. Tab.	$1^{\circ} 0'$	Logarithmic sum radius rejected			19.737751
Difference of true altitudes,	$2^{\circ} 26' 44''$	$1^{\circ} 18' 22'' = \log. \text{ fine } 8.329182$ , which multiplied by 2 is			16.658364
Half difference is	$1^{\circ} 13' 22''$				
* This falls in with direction 4th of the Table of Multipliers.	$47^{\circ} 42' 22''$			The above logarithm increased by the difference	3.079387
	$2$				3.079749
	$95^{\circ} 24' 44''$	True Distance,		Half the above logarithm is	1.539875
				Half difference of true altitudes, log. fine	8.329182
				log. fine	9.869057

# EXAMPLE VI.

Let the apparent distance of the moon's center from a star be  $118^{\circ} 32'$  when the star's apparent altitude was  $29^{\circ}$ , the moon's apparent altitude  $29^{\circ} 2'$  and her horizontal parallax  $61' 18''$ . Required their True Distance.

Moon's apparent altitude,	$29^{\circ} 2'$	Apparent distance,	$118^{\circ} 32'$	Logarithm from Tab. 9,	
Star's	$29^{\circ} 0'$	Diff. of apparent altitudes,	$0^{\circ} 2'$	Req. Tab.	9.996416
Difference of apparent altitudes,	$0^{\circ} 2'$	Sum	$118^{\circ} 34'$	Half is $59^{\circ} 17'$ log. fine	9.934349
Correction from tab. 8, Req. Tab.	$51' 53''$	Difference	$118^{\circ} 30'$	Half is $59^{\circ} 15'$ log. fine	9.934199
Star's refraction tab. 1, Req. Tab.	$1^{\circ} 42'$	Logarithmic sum radius rejected			19.864964
Difference of true altitudes,	$0^{\circ} 55' 35''$	$0^{\circ} 27' 47\frac{1}{2}'' = \log. \text{ fine } 7.907589$ , which multiplied by 2 is			15.815178
Half difference is	$0^{\circ} 27' 47\frac{1}{2}''$				
* This falls in with direction 5th of the Table of Multipliers.	$58^{\circ} 52' 35''$			The above logarithm increased by one tenth of difference	4.049786
	$2$				4.049825
	$117^{\circ} 45' 10''$	True Distance,		Half the above logarithm is	2.024913
				Half the difference of true altitudes, log. fine	7.907589
				log. fine	9.932502



## EXAMPLE VII.

Let the apparent distance of the moon's center from a star be  $87^{\circ} 10'$  when the star's apparent altitude was  $40^{\circ} 12'$ , the moon's apparent altitude  $39^{\circ} 14'$  and her horizontal parallax  $58' 9''$ . Required their True Distance.

Star's apparent altitude,	$40^{\circ} 12'$	Apparent distance,	$87^{\circ} 10'$	Logarithm from Tab. 9,	
Moon's	$39^{\circ} 14'$	Diff. of apparent altitudes,	$0^{\circ} 58'$	Req. Tab.	$9.995534$
Difference of apparent altitudes,	$0^{\circ} 58'$	Sum	$88^{\circ} 8'$	Half is $44^{\circ} 4'$ log. fine	$9.842294$
Correction from tab. 8, Req. Tab.	$1^{\circ} 43' 53''$	Difference	$86^{\circ} 12'$	Half is $43^{\circ} 6'$ log. fine	$9.834595$
Star's refraction tab. 1, Req. Tab.	$1^{\circ} 7'$	Logarithmic sum radius rejected			$19.672422$
Difference of true altitudes,	$0^{\circ} 13' 0''$	$0^{\circ} 6' 30'' = \log. \text{ fine } 7.275351$ , which multiplied by 2 is			$14.550702$
Half difference is	$0^{\circ} 6' 30''$	The above logarithm increased by one hundredth of difference			$5.121721$
		Half the above logarithm is			$2.560862$
* This falls in with direction 6th of the Table of Multipliers.	$43 \quad 18 \quad 2$	Half difference of true altitudes, log. fine			$7.275351$
	$86 \quad 36 \quad 4$	log. fine			$9.836213$
		True Distance.			

## EXAMPLE VIII.

Let the apparent distance of the moon's center from a star be  $104^{\circ} 10'$  when the star's apparent altitude was  $30^{\circ} 35'$ , the moon's apparent altitude  $29^{\circ} 40'$  and her horizontal parallax  $60' 54''$ . Required their True Distance.

Star's apparent altitude,	$30^{\circ} 35'$	Apparent distance,	$104^{\circ} 10'$	Logarithm from Tab. 9,	
Moon's	$29^{\circ} 40'$	Diff. of apparent altitudes,	$0^{\circ} 55'$	Req. Tab.	$9.996368$
Difference of apparent altitudes,	$0^{\circ} 55'$	Sum	$105^{\circ} 5'$	Half is $52^{\circ} 32' 30''$ log. fine	$9.899709$
Correction from tab. 8, Req. Tab.	$51^{\circ} 15''$	Difference	$103^{\circ} 15'$	Half is $51^{\circ} 37' 30''$ log. fine	$9.894296$
Star's refraction tab. 1, Req. Tab.	$1^{\circ} 36'$	Logarithmic sum radius rejected,			$19.790373$
Difference of true altitudes,	$0^{\circ} 2^{\circ} 9''$	$0^{\circ} 1^{\circ} 41'' = \log. \text{ fine } 6.486303$ , which multiplied by 2 is			$12.972606$
Half difference is	$0^{\circ} 1^{\circ} 41''$				$6.817767$
* This falls in with direction 7th of the Table of Multipliers.	$51 \quad 46 \quad 26$	Half the above logarithm is			$3.408884$
	$103 \quad 32 \quad 52$	Half difference of true altitudes, log. fine			$6.486303$
		log. fine			$9.895187$
		True Distance.			

## EXAMPLE IX.

Let the apparent distance of the moon's center from a star be  $72^{\circ}$  when the star's apparent altitude was  $80^{\circ} 4'$ , the moon's apparent altitude  $12^{\circ} 30'$  and her horizontal parallax  $53' 10''$ . Required their True Distance.

Star's apparent altitude,	$80^{\circ} 4'$	Apparent distance,	$72^{\circ} 0'$	Logarithm from Tab. 9,	
Moon's	$12^{\circ} 30'$	Diff. of apparent altitudes,	$67^{\circ} 34'$	Req. Tab.	$9.998737$
Difference of apparent altitudes,	$67^{\circ} 34'$	Sum	$139^{\circ} 34'$	Half is $69^{\circ} 47'$ log. fine	$9.972385$
Correction from tab. 8, Req. Tab.	$47^{\circ} 41''$	Difference	$4^{\circ} 26'$	Half is $2^{\circ} 13'$ log. fine	$8.587469$
Star's refraction tab. 1, Req. Tab.	$10'$	+ Logarithmic sum radius rejected			$18.558591$
Difference of true altitudes,	$66^{\circ} 46' 9''$	Half the above logarithm is			$9.279296$
Half difference is	$33^{\circ} 23' 5''$	$33^{\circ} 23' 5'' = \log. \text{ fine } 9.740566$ , which multiplied by 2 is			$19.481132$
		Logarithmic sum radius rejected			$18.558591$
* This falls in with direction 1st of the Table of Multipliers.	$35 \quad 36 \quad 23$	$8.366 = 0.922541$			
	$71 \quad 12 \quad 46$	$9.366 = 0.971574$			
		Half the above logarithm is			$0.485787$
		Half the logarithmic sum radius rejected			$9.279296$
		log. sum			$9.765083$
		True Distance.			



FINIS.